

According to the decompilation of the Ciso Vigenere hash algorithm, when the password length is less than 16 the idea behind Ciso Vigenere hash algorithm is:

Let p be the password that the user types.
Let hp be the hardcoded password in the code of Packet Tracer.
Let lp be the length of the user input password.
Let h be the hash value obtained from the custom algorithm.
So that:

$$\begin{aligned}
& \forall h \forall lp \forall hp [(hp = \\
& (d, s, f, d, ;, k, f, o, A, , , , i, y, e, w, r, k, l, d, J, K, D, H, S, U, B, s, g, v, c, a, 6, 9, 8, 3, 4, n, c, x, v), \\
& 0 < lp < 16, \\
& h_0 = 0, \\
& h_1 = 8, \\
& h = \\
& \Sigma_{i=2}^{lp} \begin{cases} ((p_i \oplus hp_{8+i}) \ggg 4) + 0x30, & \text{if } (h_i \oplus hp_{i+8} \wedge 0xfffffffff0 < 0xa0) \text{ and if } i \equiv 0 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \ggg 4) + 0x37, & \text{if } (h_i \oplus hp_{i+8} \wedge 0xfffffffff0 \geq 0xa0) \text{ and if } i \equiv 0 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \wedge 0xf) + 0x30, & \text{if } (h_i \oplus hp_{i+8} \wedge 0xf < 0x0a) \text{ and if } i \equiv 1 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \wedge 0xf) + 0x37, & \text{if } (h_i \oplus hp_{i+8} \wedge 0xf \geq 0x0a) \text{ and if } i \equiv 1 \pmod{2} \end{cases} \\
&) \implies \#p[p = \mathbf{rev}(h)](0)
\end{aligned}$$

Let's start by proving

$$\begin{aligned}
& \forall h \forall lp \forall hp [(hp = \\
& (d, s, f, d, ;, k, f, o, A, , , , i, y, e, w, r, k, l, d, J, K, D, H, S, U, B, s, g, v, c, a, 6, 9, 8, 3, 4, n, c, x, v), \\
& 0 < lp < 16, \\
& h_0 = 0, \\
& h_1 = 8, \\
& h = \\
& \Sigma_{i=2}^{lp} \begin{cases} ((p_i \oplus hp_{8+i}) \ggg 4) + 0x30, & \text{if } (h_i \oplus hp_{i+8} \wedge 0xfffffffff0 < 0xa0) \text{ and if } i \equiv 0 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \ggg 4) + 0x37, & \text{if } (h_i \oplus hp_{i+8} \wedge 0xfffffffff0 \geq 0xa0) \text{ and if } i \equiv 0 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \wedge 0xf) + 0x30, & \text{if } (h_i \oplus hp_{i+8} \wedge 0xf < 0x0a) \text{ and if } i \equiv 1 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \wedge 0xf) + 0x37, & \text{if } (h_i \oplus hp_{i+8} \wedge 0xf \geq 0x0a) \text{ and if } i \equiv 1 \pmod{2} \end{cases}
\end{aligned}$$

) $\implies \nexists p[p = \mathbf{rev}(h)]$
 (0)

I/ substraction to reverse the addition

$\forall x[(x = y + z) \implies (y = ez)]$ then it follow that as the previous part of the function contains: $h = x + 0x30$, then $h - 0x30 = x$ so

$\exists rev(h)[rev(H(p)) = p - 0x30]$

II/ exclusive or

According to the boolean algebra about the exclusive logical or operation,

$\forall x[y = (x \oplus x) \implies (y = 0)]$.

Then as $xlat \oplus xlat = 0$, and as $p \oplus 0 = p$, we know that the original password $p = (xlat \oplus h)$.

III/ rotating 4 first to 4 last bits

$\forall x[(x \ggg y) \implies (x \lll y = x)]$.

Then as $z = (x \ggg y) = (x \lll y)$, we know that the original password $p = H(p) \lll 4$.

IV/ unmasking different signatures (recurrent marks) in the password modification

In the previous chapter one 'I/ substraction to reverse the addition', we told we can reverse the previous addition. We still need to guess which addition/substraction has been done previously.

As both addition values are made depending to: if

$(p_l \wedge 0xf0 < 0xa0) \implies (p_l \wedge 0xf0 + 0x30)$ or else

$(p_l \wedge 0xf0 > 0xa0) \implies (p_l \wedge 0xf0 + 0x37)$

if $(p_r \wedge 0x0f < 0x0a) \implies (p_r \wedge 0x0f + 0x30)$ or else

$(p_r \wedge 0x0f > 0xa0) \implies (p_r \wedge 0x0f + 0x37)$

So if the out has the 4 four bits value so that:

$x \in \{x|(0xf0x) \leq 0xa0\} \implies y = x + 0x30$

So if the out has the 4 four bits value so that:

$x \in \{x|(0xf0x) > 0xa0\} \implies y = x + 0x37$

So if the out has the 4 four first bits value so that:

$x \in \{x|(0x0fx) \leq 0x0a\} \implies y = x + 0x30$

So if the out has the 4 four first bits value so that:

$$x \in \{x | (0x0fx) > 0x0a\} \implies y = x + 0x37$$

first byte:

$$\text{as } 0xa0 < 0xf0 + 0x30 < y$$

$$-1 : \forall y \in H(x) [(x \in \{x | 0xa0 < x\}) \implies (y \in \{y | 0x00 < y < 0xa7\})]$$

$$-2 : \forall y \in H(x) [(x \in \{x | x < 0xa0\}) \implies (y \in \{y | 0xc0 < y\})]$$

second byte: as $0xa0 < 0x0f + 0x30 < y$

$$-1 : \forall y \in H(x) [(x \in \{x | x < 0xa0\}) \implies (y \in \{y | 0x3a < y\})]$$

$$-2 : \forall y \in H(x) [(x \in \{x | 0x0a < x\}) \implies (y \in \{y | y < 0x4a\})]$$

Then for both of any subnumber:

$$\text{that } \forall y = H(x), x \in \{x | x \leq 0xa\} \implies y = x + 0x30$$

$$\text{and that } \forall y = H(x), x \in \{x | x > 0xa\} \implies y = x + 0x37$$

It follows:

$$\text{that } \forall y = H(x) [(y \in \{y | 0 < y \leq 0x0a + 0x30\}) \implies (x = y - 0x30)] \text{ then}$$

$$0 < x < 0x0a$$

$$\text{and that } \forall y = H(x) [(y \in \{y | 0 < y \leq 0x0a + 0x37\}) \implies (x = y - 0x30)] \text{ then}$$

$$0x0a \leq x$$

V/ commutativity:

Addition, subtraction and \oplus are commutative.

VI/ proof

Then we have already proven each piece of the theorem so that: $hp =$

$$(d, s, f, d, ;, k, f, o, A, , , , i, y, e, w, r, k, l, d, J, K, D, H, S, U, B, s, g, v, c, a, 6, 9, 8, 3, 4, n, c, x, v) \implies$$

$$(\forall x \in hp [0 \geq x0 \geq 256 \implies x \in hp])$$

then:

Let p be the password that the user types.

Let hp be the hardcoded password in the code of Packet Tracer.

Let lp be the length of the user input password.

Let h be the hash value obtained from the custom algorithm.

So that:

$$\forall h \forall lp \forall hp [(hp \in N \wedge 0 \geq hp,$$

$$0 < lp < 16,$$

$$\begin{aligned}
&h_0 = 0, \\
&h_1 = 8, \\
&h = \\
&\sum_{i=2}^{lp} \left\{ \begin{array}{ll}
(((p_i \oplus hp_{i+8}) \lll 4) - 0x30), & \text{if } h_i < 0xa0 \text{ and if } i \equiv 0 \pmod{2} \\
(((p_i \oplus hp_{i+8}) \lll 4) - 0x37), & \text{if } h_i \geq 0xa0 \text{ and if } i \equiv 0 \pmod{2} \\
(((p_i \oplus hp_{i+8}) \wedge 0xfffffffff0) - 0x30), & \text{if } h_i < 0x0a \text{ and if } i \equiv 1 \pmod{2} \\
(((p_i \oplus hp_{i+8}) \wedge 0xfffffffff0) - 0x37), & \text{if } h_i \geq 0x0a \text{ and if } i \equiv 1 \pmod{2}
\end{array} \right. \\
&) \implies \forall p[p = \mathbf{rev}(h)]
\end{aligned}$$